$$\sinh(z) = \frac{e^z - e^{-z}}{2}$$
$$= -i\sin(iz)$$
$$= \sum_{n=0}^{\infty} \frac{z^{2n+1}}{(2n+1)!}$$